

## Math 208 Homework 7.

Problems from P.M. Fitzpatrick, Advanced Calculus.

Section 9.1, p.239: Problems: 1, 3, 7, 8

Section 9.2, p.244 : Problems: 1, 2, 3, 4 ,6

and the following problems:

**Problem 1.** Let  $\{b_n\}$  be a sequence that converges to the number  $b$ . Show that the series

$$\sum_{n=1}^{\infty} (b_{n+1} - b_n) = b - b_1.$$

**Problem 2.** Show that if the series

$$\sum_{n=1}^{\infty} (a_n)^2$$

is convergent, then the series

$$\sum_{n=1}^{\infty} \frac{|a_n|}{n}$$

is also convergent.

**Problem 3.** Show the convergence of the series

$$\sum_{n=1}^{\infty} \frac{1}{n^2}$$

by using Cauchy's criterion.